

M. P. SHAH ARTS & SCIENCE COLLEGE, SURENDRANAGAR.

Assignment-1 B. Sc. Semester-I (2019-20)

Mathematics Paper- 01(A)

Date of Submission: 13/08/2019

Time: 12:00 to 12:30

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**Q. 1 Answer the following questions.**

1) State and prove Rolle's theorem.

2) State and prove Cauchy's mean value theorem.

3) For  $f(x) = \log x$  show that  $\frac{b-a}{b} < \log \frac{b}{a} < \frac{b-a}{a}$ , where  $0 < a < b$ .

4) Prove that if  $f'(x) < 0, \forall x \in (a, b)$ , then  $f$  is strictly increasing in  $(a, b)$ .

5) Expand  $e^x$  in ascending powers of  $(x - 2)$ .

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**Assignment-2 B. Sc. Semester-I (2019-20)**

**Mathematics Paper- 01(A)**

**Date of Submission: 27/08/2019**

**Time: 12:00 to 12:30**

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**Q. 1 Answer the following questions.**

1) Evaluate  $\lim_{x \rightarrow \frac{\pi}{2}} \left( \cot^2 x - \frac{1}{x^2} \right)$ .

2) If  $\lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos^2 x}{a - b \operatorname{cosec} x} = 1$ , then find value of  $a$  and  $b$ .

3) Solve  $(x^2 + y^2)dx + 2xydy = 0$ .

4) Prove that the necessary and sufficient conditions for the differential equation

$$M(x, y)dx + N(x, y)dy = 0 \text{ to be exact is } \frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}.$$

5) Solve  $y - 2px = \tan^{-1}(xp^2)$ .

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Assignment-3 B. Sc. Semester-I (2019-20)

Mathematics Paper- 01(A)

Date of Submission: 06/09/2019

Time: 12:00 to 12:30

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**Q. 1 Answer the following questions.**

1) Solve:  $\frac{d^4y}{dx^4} - 2\frac{d^3y}{dx^3} + 5\frac{d^2y}{dx^2} - 8\frac{dy}{dx} + 4y = 0.$

2) Solve:  $(D^4 + 4)y = 0.$

3) Solve:  $\frac{d^2y}{dx^2} - 7\frac{dy}{dx} + 12y = e^{5x}.$

4) Solve:  $\frac{d^3y}{dx^3} - 12\frac{d^2y}{dx^2} + 6\frac{dy}{dx} - 8y = e^{2x}.$

5) Prove that  $\frac{1}{D^2+a^2} \cos ax = \frac{x}{2a} \sin ax, \frac{1}{D^2+a^2} \sin ax = -\frac{x}{2a} \cos ax.$

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**Assignment-4 B. Sc. Semester-I (2019-20)**

**Mathematics Paper- 01(A)**

**Date of Submission: 14/09/2019**

**Time: 12:00 to 12:30**

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**Q. 1 Answer the following questions.**

1) Solve:  $x^2 \frac{d^2y}{dx^2} + y = 3x^2$ .

2) Solve:  $x^2 \frac{d^2y}{dx^2} + 7x \frac{dy}{dx} + 5y = x^5$ .

3) Solve:  $(x^3 D^3 + 2x^3 D^2 + 2)y = 10 \left(x + \frac{1}{x}\right)$ .

4) Solve:  $x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + y = 2 \log x$ .

5) Solve:  $x^3 \frac{d^3y}{dx^3} + 3x^2 \frac{d^2y}{dx^2} - 6x \frac{dy}{dx} + 6y = \left(x^2 - \frac{1}{x^2}\right)^2$ .